

# Structural Transformation and Aggregate Productivity in China

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# Background

- Unprecedented growth during the past thirty decades
- This impressive growth performance accompanied important structural transformations:

$$\frac{Y}{L} = \sum_i \frac{L_i}{L} \frac{Y_i}{L_i}, \quad i \in \{a, m, s\}$$

# Motivation

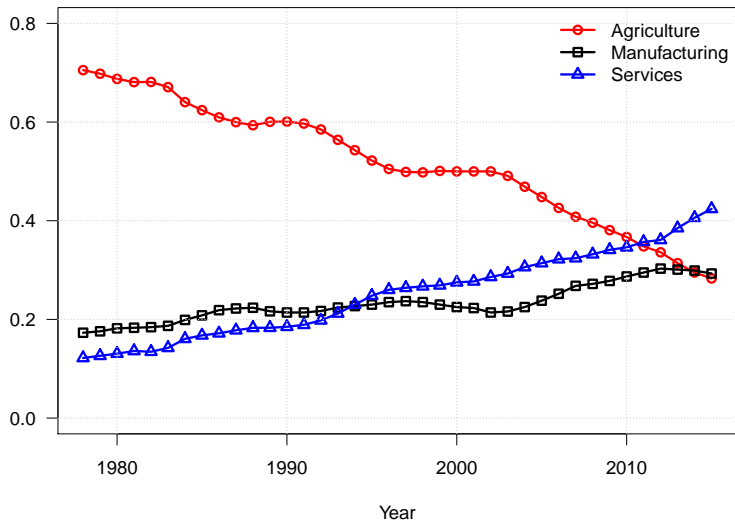
- What theories can account for the facts of structural transformation in China?
- Help understanding the role of structural transformation in China's productivity growth.
- Help understanding China's growth miracle in the past and growth potential in the future.

# Introduction

- Test major structural change models with data:
  - Generalized Stone-Geary preference
  - Non-homothetic CES preference
  - Price independent generalized linearity preference
- Measure sectoral labor productivity using the Non-homothetic CES preference

# Facts of Structural Transformation in China

## Employment Share



# Traditional Structural Change Theory

- Generalized Stone-Geary utility function:

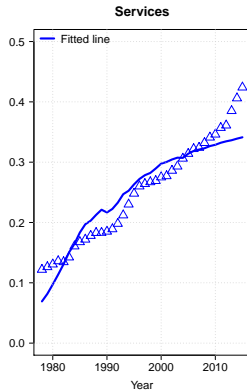
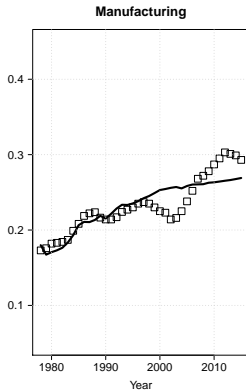
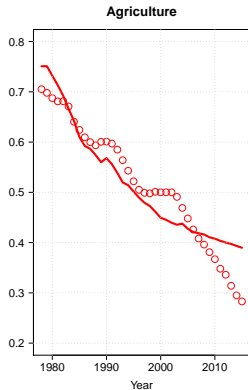
$$u(c) = \left[ \phi_a (c_a + \bar{c}_a)^{\frac{\epsilon-1}{\epsilon}} + \phi_m (c_m + \bar{c}_m)^{\frac{\epsilon-1}{\epsilon}} + \phi_s (c_s + \bar{c}_s)^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon-1}},$$

where  $\phi_i \in (0, 1)$  and  $\sum_i \phi_i = 1$ .

- Stone-Geary parameter:  $\bar{c}_a < 0$ ,  $\bar{c}_m = 0$ ,  $\bar{c}_s > 0$
- Elasticity of substitution:  $0 < \epsilon < 1$
- Equilibrium

$$\frac{L_i}{L} = \frac{\phi_i p_i^{1-\epsilon}}{\sum_i \phi_i p_i^{1-\epsilon}} \left( 1 + \frac{\sum_i p_i \bar{c}_i}{\sum_i p_i c_i} \right) - \frac{p_i \bar{c}_i}{\sum_i p_i c_i}$$

# Disadvantages of Generalized Stone-Geary Utility



## Alternative Theories

- Boppart (2014), Alder et al (2017): Price independent generalized linearity preference (PIGL)

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$$v(e, p) = \frac{1}{\epsilon} \left[ \frac{e - f_1(p)}{f_2(p)} \right]^\epsilon - \frac{1}{\epsilon} + f_3(p),$$

where

$$f_1(p) = \tau p_a^{1-\rho} p_s^\rho$$

$$f_2(p) = p_m^{1-\theta} p_s^\theta$$

$$f_3(p) = - \left( \frac{\gamma_1}{\psi_1} \left[ \frac{p_a}{p_s} \right]^{\psi_1} + \frac{\gamma_2}{\psi_2} \left[ \frac{p_m}{p_s} \right]^{\psi_2} \right)$$



# Alternative Theories

- Comin et al (2015): Non-homothetic CES preference

$$\phi_a^\epsilon c_a^{\frac{\mu_a - \epsilon}{\epsilon}} c_a^{\frac{\epsilon - 1}{\epsilon}} + \phi_m^\epsilon c_m^{\frac{\mu_m - \epsilon}{\epsilon}} c_m^{\frac{\epsilon - 1}{\epsilon}} + \phi_s^\epsilon c_s^{\frac{\mu_s - \epsilon}{\epsilon}} c_s^{\frac{\epsilon - 1}{\epsilon}} = 1$$

- $\mu_i$ : income elasticity parameter for good  $i$  (CES if  $\mu_i = 1$ )
- Constant elasticity of the relative demand for two different goods with respect to aggregate consumption:

$$\frac{\partial \ln(c_i/c_j)}{\partial \ln c} = \mu_i - \mu_j$$

- Constant elasticity of substitution:

$$\frac{\partial \ln(c_i/c_j)}{\partial \ln(p_j/p_i)} = \epsilon$$

# Model Assessment

- Non-homothetic CES

$$\frac{L_i}{L_j} = \frac{\phi_i}{\phi_j} \left( \frac{p_i}{p_j} \right)^{1-\epsilon} c^{\mu_i - \mu_j}$$

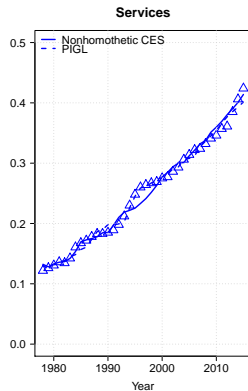
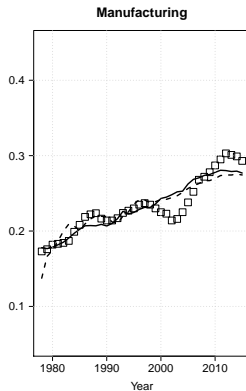
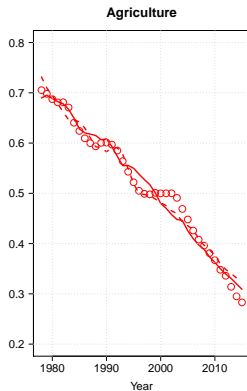
- PIGL

$$\frac{L_a}{L} = (1 - \rho) \frac{f_1(p)}{e} + \gamma_1 \left( \frac{p_a}{p_s} \right)^{\psi_1} \left[ \frac{e - f_1(p)}{f_2(p)} \right]^{1-\epsilon} \frac{f_2(p)}{e}$$

$$\frac{L_m}{L} = -(1 - \theta) \frac{f_1(p)}{e} + (1 - \theta) + \gamma_2 \left[ \frac{p_m}{p_s} \right]^{\psi_2} \left[ \frac{e - f_1(p)}{f_2(p)} \right]^{1-\epsilon} \frac{f_2(p)}{e}$$

$$\frac{L_s}{L} = -(\rho - \theta) \frac{f_1(p)}{e} + \theta - \left( \gamma_1 \left[ \frac{p_a}{p_s} \right]^{\psi_1} + \gamma_2 \left[ \frac{p_m}{p_s} \right]^{\psi_2} \right) \left[ \frac{e - f_1(p)}{f_2(p)} \right]^{1-\epsilon} \frac{f_2(p)}{e}$$

# Fitting Results



## Fitting Results

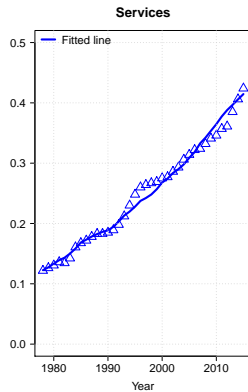
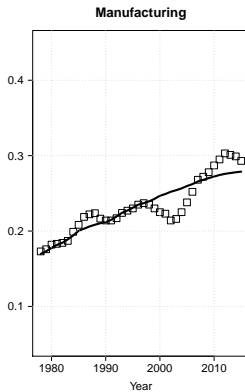
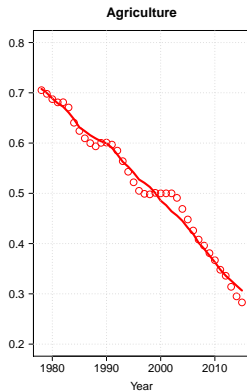
- Assessment

	(1)	(2)	(3)
SSR	0.04717	0.01282	0.01369
$k$	5	5	8
AICc	-5.04	-6.34	-5.94

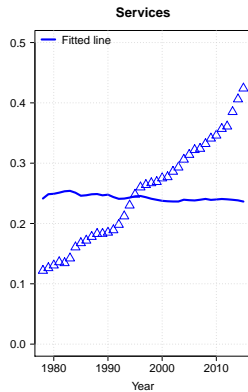
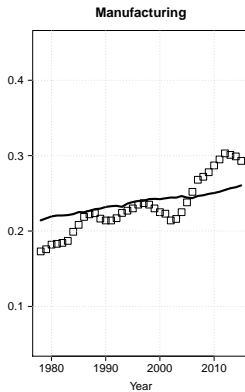
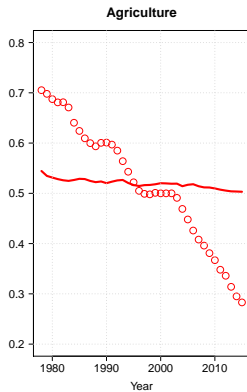
(1): Stone-Geary CES; (2): Non-homothetic CES; (3) PIGL

- Verdicts: Non-homothetic CES

# Income Effect



# Price Effect



# The Quantitative Model

- Preferences

$$\max \sum_{t=0}^{\infty} \beta^t \frac{c_t^{1-\sigma} - 1}{1-\sigma},$$

s.t.

$$\sum_{i \in \{a, m, s\}} \phi_i^{\frac{1}{\epsilon}} c_i^{\frac{\mu_i - \epsilon}{\epsilon}} c_i^{\frac{\epsilon - 1}{\epsilon}} = 1,$$

and

$$a_{t+1} + \sum_i p_{it} c_{it} = w_t + (1 + r_t) a_t$$

- Technologies:

$$Y_i = A_i L_i$$

- Equilibrium:

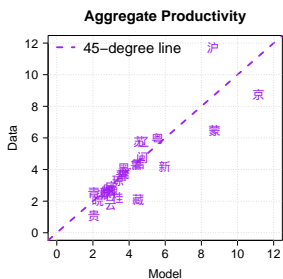
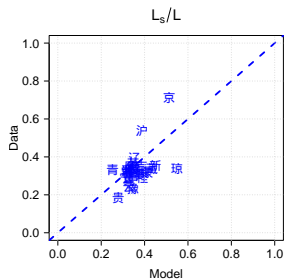
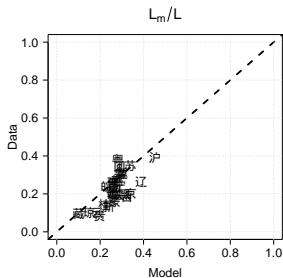
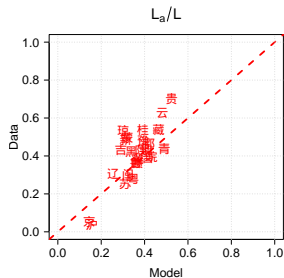
$$\frac{L_i}{L} = \phi_i c_i^{\mu_i - \epsilon} A_i^{\epsilon - 1}$$

# Calibration

Parameter	Value	Description
$\phi_a$	0.41	weight of agricultural sector
$\phi_s$	0.30	weight of service sector
$\epsilon$	0.68	elasticity of substitution
$\mu_a$	0.79	income elasticity parameter of agriculture
$\mu_m$	2.40	income elasticity parameter of manufacturing
$\mu_s$	2.82	income elasticity parameter of services

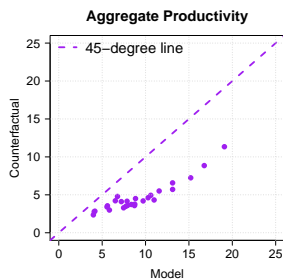
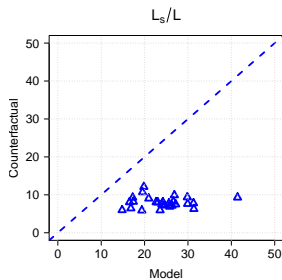
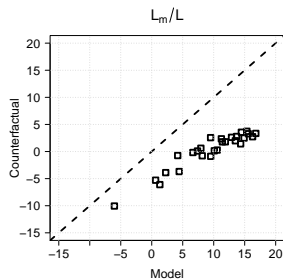
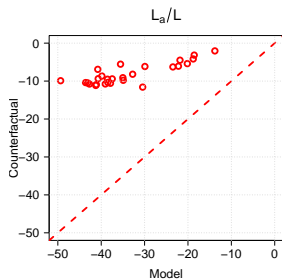


# Calibration Assessment: Last Period

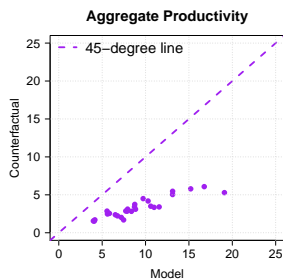
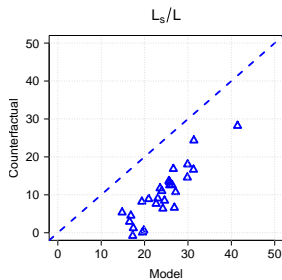
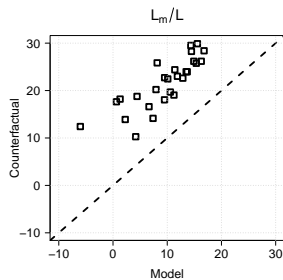
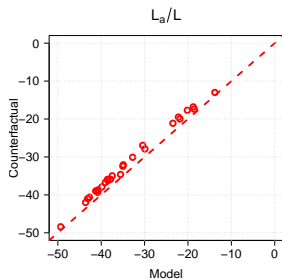




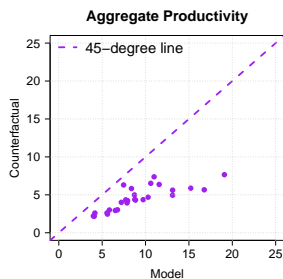
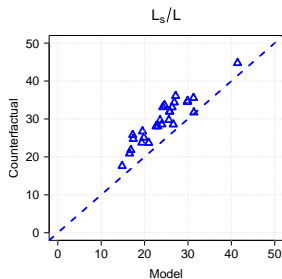
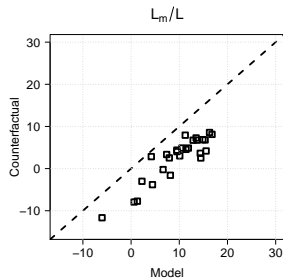
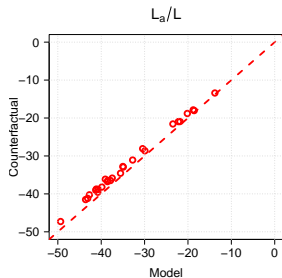
# Counterfactual Analysis: $\gamma_a = 0$



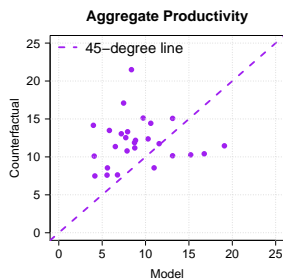
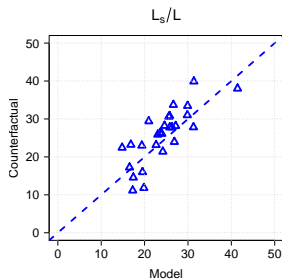
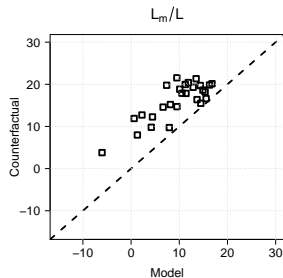
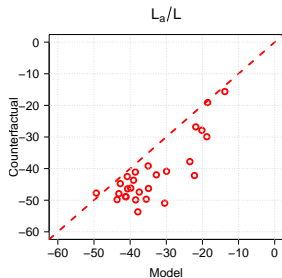
# Counterfactual Analysis: $\gamma_m = 0$



# Counterfactual Analysis: $\gamma_s = 0$



# Counterfactual Analysis: $\gamma_i = \gamma^{national}$



# Counterfactual Analysis

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-33.75	9.59	24.17	9.11	7.79
Counterfactual:					
(1) $\gamma_a = 0$	-8.19	0.22	7.97	4.61	5.76
(2) $\gamma_m = 0$	-31.67	21.56	10.12	3.32	4.85
(3) $\gamma_s = 0$	-32.07	2.51	29.55	4.53	5.73
(4) $\gamma_i = \gamma^{national}$	-41.74	16.09	25.65	11.98	8.83

# Counterfactual Analysis

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	Annualized rate (%)
Model	-33.75	9.59	24.17	9.11	7.79
Counterfactual:					
(1) $\gamma_a = \gamma_a^{national}$	-31.59	8.89	22.71	8.54	7.63
(2) $\gamma_m = \gamma_m^{national}$	-33.60	10.99	22.60	8.02	7.44
(3) $\gamma_s = \gamma_s^{national}$	-33.52	8.34	25.18	7.70	7.39
(4) $\gamma_i = \gamma_i^{national}$	-31.15	9.01	22.14	6.49	6.85



## Counterfactual Analysis: by Groups

- By growth rate (GDP per capita from 1978 to 2008):
  - high (9.40% on average): Guangdong, Jiangsu, Fujian, Inner Mongolia, Shandong, Shanghai, Hebei, Hainan
  - median (7.63% on average): Xinjiang, Hubei, Hunan, Jiangxi, Shanxi, Shaanxi, Anhui, ...
  - low (5.95% on average): Ningxia, Heilongjiang, Qinghai, Guizhou

# Counterfactual Analysis: High Growth Rate

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-38.28	11.85	26.43	12.95	9.01
Counterfactual:					
(1) $\gamma_a = 0$	-9.04	1.01	8.04	6.46	6.74
(2) $\gamma_m = 0$	-36.30	25.81	10.48	4.80	5.97
(3) $\gamma_s = 0$	-36.33	2.53	33.80	5.52	6.34
(4) $\gamma_i = \gamma^{national}$	-41.21	15.59	25.62	11.08	8.59

# Counterfactual Analysis: High Growth Rate

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-38.28	11.85	26.43	12.95	9.01
Counterfactual:					
(1) $\gamma_a = \gamma_a^{national}$	-31.72	9.60	22.13	11.30	8.53
(2) $\gamma_m = \gamma_m^{national}$	-38.01	14.42	23.60	10.44	8.36
(3) $\gamma_s = \gamma_s^{national}$	-37.62	8.44	29.17	8.93	7.88
(4) $\gamma_i = \gamma_i^{national}$	-30.63	8.61	22.02	5.96	6.62

# Counterfactual Analysis: Median Growth Rate

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-33.58	8.95	24.63	8.08	7.55
Counterfactual:					
(1) $\gamma_a = 0$	-8.05	-0.08	8.13	4.04	5.51
(2) $\gamma_m = 0$	-31.58	20.65	10.93	2.90	4.58
(3) $\gamma_s = 0$	-31.98	2.54	29.44	4.46	5.72
(4) $\gamma_i = \gamma^{national}$	-42.24	15.86	26.38	12.27	8.89

# Counterfactual Analysis: Median Growth Rate

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-33.58	8.95	24.63	8.08	7.55
Counterfactual:					
(1) $\gamma_a = \gamma_a^{national}$	-31.85	8.37	23.48	7.74	7.42
(2) $\gamma_m = \gamma_m^{national}$	-33.45	10.15	23.31	7.49	7.29
(3) $\gamma_s = \gamma_s^{national}$	-33.49	8.31	25.17	7.56	7.35
(4) $\gamma_i = \gamma_i^{national}$	-31.60	8.90	22.70	6.77	6.94

# Counterfactual Analysis: Low Growth Rate

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-25.34	7.42	17.92	5.28	6.24
Counterfactual:					
(1) $\gamma_a = 0$	-7.00	-0.24	7.24	3.06	4.74
(2) $\gamma_m = 0$	-22.78	16.44	6.33	1.92	3.60
(3) $\gamma_s = 0$	-23.88	2.40	21.48	2.85	4.54
(4) $\gamma_i = \gamma^{national}$	-40.97	17.97	23.00	12.71	9.09

# Counterfactual Analysis: Low Growth Rate

	Change in labor share			Change in aggregate productivity	
	Agriculture	Manufacturing	Services	Total	annualized rate (%)
Model	-25.34	7.42	17.92	5.28	6.24
Counterfactual:					
(1) $\gamma_a = \gamma_a^{national}$	-30.37	9.41	20.96	6.01	6.61
(2) $\gamma_m = \gamma_m^{national}$	-25.34	7.34	18.00	5.20	6.22
(3) $\gamma_s = \gamma_s^{national}$	-25.50	8.26	17.24	5.82	6.58
(4) $\gamma_i = \gamma_i^{national}$	-30.53	10.24	20.29	6.53	6.94